

PORTFOLIO MANAGEMENT

CLASS 5

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Date

↳ always ignored but focus on CAPM

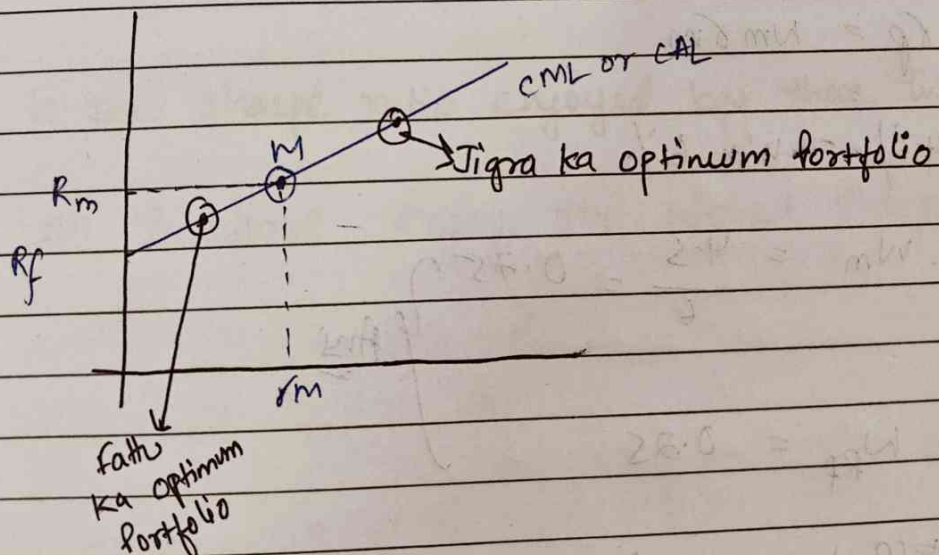
PART-II → CAPITAL MARKET THEORY (CMT) leads us to Capital Asset Pricing Model (CAPM)

CMT

↓

All investors are assumed to be rational (risk averse). So, they invest in the most diversified portfolio i.e. Market Portfolio & combine that with risk free lending (fattu) or risk free borrowing (Jigra) & everyone enjoys the highest Sharpe ratio $\left[\frac{R_m - R_f}{\sigma_m} \right]$ on the CAL or CML.

$$R_p = R_f + \left[\frac{R_m - R_f}{\sigma_m} \right] \sigma_p$$



These portfolios that lie on the CML are called Efficient Portfolios.

Combination of MKT & Rf

$$\sigma_p = w_m \sigma_m$$

∵ Rf ka sd = 0 ∴ only $w_m \sigma_m$

→ weighted avg

$$R_p = W_m R_m + (1 - W_m) R_f$$

Risky

Never came
in
Exam
but given
in RFP /
MTP

~~Q. No. 1~~ Example :-

Assume that we live in the CMT or CAPM world :-

Risk free rate return = 5%

Expected return on mkt portfolio = 14%

S.d of market portfolio = 6%

Q. No. 1 Mr. X wants to construct an efficient portfolio with sd of 4.5%. Construct the portfolio and calculate expected return on the portfolio?

Soln:-

$$\sigma_p = W_m \sigma_m$$

$$4.5\% = W_m 6\%$$

$$\therefore W_m = \frac{4.5}{6} = 0.75$$

$$\therefore W_{Rf} = 0.25$$

$$E(R_p) = 0.75 \times 14 + 0.25 \times 5$$

$$= 11.75\% \quad (\text{Ans}) \quad (\text{Factor})$$

Q.No.2 Mr. Y wants to construct an efficient portfolio with Expected Return = 21%. Construct the portfolio and find out SD of the portfolio.

Soln:- $E(R_p) = W_m \times R_m + (1 - W_m) R_f$

$$21 = W_m \times 14 + (1 - W_m) 5$$

$$21 = 14W_m + 5 - 5W_m$$

$$16 = 9W_m$$

$$W_m = \frac{16}{9} = 1.78 \text{ approx}$$

$$W_{Rf} = 0 - 0.78 \text{ (short sell) / Risk free borrowing}$$

$$\sigma_p = W_m \times \sigma_m$$

$$= 1.78 \times 6$$

$$= 10.67\% \text{ (Ans) (Igra)}$$

Q.No.3 What is the Sharpe ratio enjoyed by these two investors on CML

Soln:- All investors enjoy the highest Sharpe ratio

$$= \frac{R_m - R_f}{\sigma_m}$$

$$= \frac{14 - 5}{6} = 1.5$$

Q4. State the Equation of the CML or CAL?

$$R_p = R_f + \text{Sharpe ratio} \times \sigma_p$$

$$R_p = 5 + 1.5 \sigma_p \rightarrow \text{same ans will come (11.75\%)}$$

CAPM → Pricing model [cap assets (stock) ka price kaise nikalte hai]
 → cos. internal risk ^{non-diversifiable}
 unsystematic risk is irrelevant by BCF
 only systematic risk is imp (economy risk is imp)
 non-diversifiable

1. Pricing Model

if CF are certain
↓
discounted @ Rf

P_0 or $IV_0 = PV$ of Exp future CF's discounted @ R_e
 ∴ ~~CFs~~ CFs are uncertain

$$= \frac{E(CF_1)}{1+R_e} + \frac{E(CF_2)}{(1+R_e)^2} + \dots + \infty$$

Required rate of return

$$= R_f + \text{risk Premium (RP)}$$

$$= R_f + \text{Systematic Risk Premium (SRP)}$$

$$R_e = R_f + (R_m - R_f) \beta_e$$

market jo 1% se change hogi to stock ki price 1% se change hogi

SRP → Systematic Risk ke badle
 Extra compensation required

volatility ↑

$$\text{Risk} = \text{Systematic Risk} + \text{Unsystematic Risk}$$

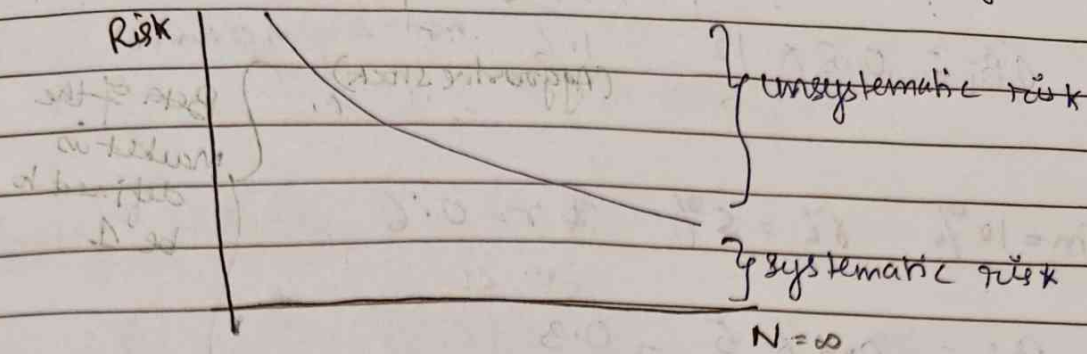
↓
 Economy wide risk
 or
 Market Risk
 or
 Non-Diversifiable risk

↓
 Company or Firm specific Risk
 or
 Diversifiable Risk
 or
 Idiosyncratic Risk

Why unsystematic risk is irrelevant in CAPM world?

Because investors invest in a combination of market & Rf. Since market portfolio is fully diversified,

unsystematic risk gets cancelled and therefore irrelevant.



Please Refer to 'N' stock worldwala sum in the last class.

$$R_e = R_f + SRP$$

Systematic Risk of a stock

Isko Capture कैसे करें?

$\beta \Rightarrow$ Sensitivity of stock Return to Market Return

↑
Market
Tab R_m 1% change hoga, To stock ka return (R_i) ki % change hoga?

$$\beta = \sigma \times \text{sd ratio} \rightarrow \frac{\sigma_{\text{stock}}}{\sigma_{\text{mkt}}}$$

$$\beta = r_{im} \times \frac{\sigma_i}{\sigma_m}$$

stock return & market return

Ex: $r_m = 6\%$ $r_i = 9\%$ & $\sigma = 0.9$

stock $\beta_i = 0.9 \times \frac{9}{6} = 1.35$ (Aggressive stock)

Ex: $r_m = 6\%$, $r_i = 12\%$ & $r = 0.8$

stock

$$\beta_i = 0.8 \times \frac{12}{6} = 1.6 \quad (\text{Aggressive stock})$$

Beta of the market is defined to be 1

Ex: $r_m = 10\%$, $r_i = 5\%$ & $r = 0.6$

stock

$$\beta_i = 0.6 \times \frac{5}{10} = 0.3 \quad (\text{Defensive stock})$$

One more formula of " β "

$$\beta_i = r \times \frac{\sigma_i}{\sigma_m}$$

$$\therefore \beta_i = r \times \frac{\sigma_i \times \sigma_m}{\sigma_m \times \sigma_m}$$

$$\therefore \beta_i = \frac{\text{Covariance}(i, m)}{\sigma_m^2}$$

↓
Pone

= Uppar mein stock ka market ke sath covariance
Neeche mein market ka variance

One more formula of β

β is slope = Rate of change of stock wrt. market

$$= \frac{Y_2 - Y_1}{X_2 - X_1}$$

$$= \frac{\Delta Y}{\Delta X}$$

$$= \frac{\Delta R_i}{\Delta R_m}$$
 Change in stock return
 Change in market return

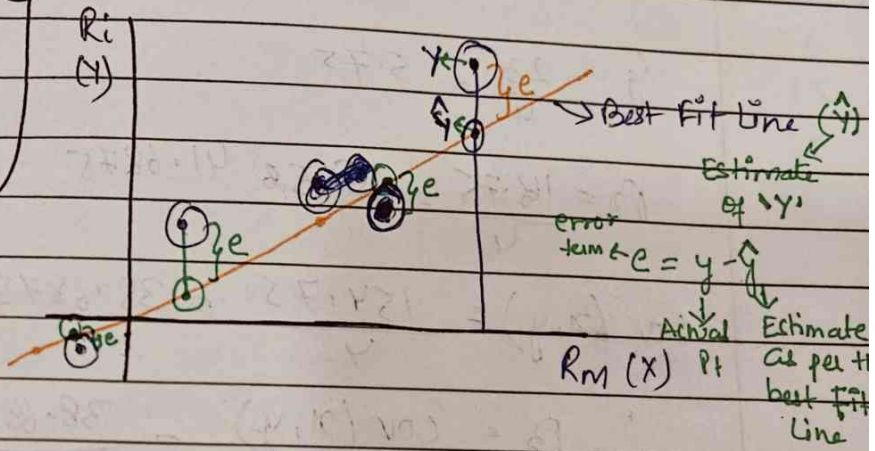
When to use this?

We use this only when two data points are given

finally statistics

Yrs	R_m	R_i
1	10%	6%
2	-2%	-4%
3	12%	9%
4	15%	12%

Plot



This Best fit line is known as the characteristic line:

$$R_i^A = \alpha_i + \beta_i R_m$$

$$\hat{y} = a + bx$$

$\hat{y}$ is R_i^A
 a is intercept
 b is beta

$$b = \frac{\sum xy}{\sum x^2} \quad \text{or} \quad \frac{\text{Cov}(x, y)}{\sigma_x^2}$$

$$a = \bar{y} - b\bar{x}$$

α = No significance

Ex:	Yrs	$R_m(X)$	$R_i(Y)$	$x - \bar{x}$	$y - \bar{y}$	$(x - \bar{x})^2$	$(y - \bar{y})^2$	$(x - \bar{x})(y - \bar{y})$
	1	10	6	1.25	0.25	1.5625	0.0625	0.3125
	2	-2	-4	-10.75	-9.75	115.5625	95.0625	1048.125
	3	12	9	3.25	3.25	10.5625	10.5625	10.5625
	4	15	12	6.25	6.25	39.0625	39.0625	39.0625
		<u>35</u>	<u>23</u>			<u>166.75</u>	<u>144.75</u>	<u>154.75</u>

$$\bar{x} = 8.75 = \frac{35}{4}$$

$$\bar{y} = \frac{23}{4} = 5.75$$

$$\sigma_x = \frac{166.75}{4} = 41.6875$$

$$\text{cov}(x, y) = \frac{154.75}{4} = 38.6875$$

$$\therefore \rho = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y} = \frac{38.6875}{41.6875}$$

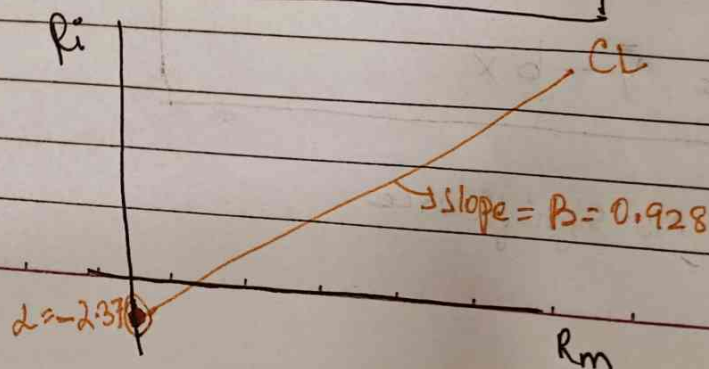
$$\rho = 0.928 \rightarrow \text{Defensive stock}$$

$$\alpha = \bar{y} - b\bar{x}$$

$$= 5.75 - 0.928 \times 8.75$$

$$= -2.37$$

$$\boxed{R_i = -2.37 + 0.928 R_m}$$



Ex ante data

Ex:

Prob	$R_m(x)$	$R_i(y)$
0.4	20%	10%
0.5	30%	40%
0.1	40%	60%

} Derive the equation of the CL

P	$R_m(x)$	$R_i(y)$	P_x	P_y	$(x-\bar{x})$	$(y-\bar{y})$	$P(x-\bar{x})^2$	$P(y-\bar{y})^2$	$P(x-\bar{x})(y-\bar{y})$
0.4	20	10	8	4	-7	-20	19.6	160	56
0.5	30	40	15	20	3	10	4.5	50	15
0.1	40	60	4	6	13	30	16.9	90	39
			27	30			41	300	110

$$\bar{x} = 27\%$$

$$\sigma_x^2 = 41$$

$$\text{Cov}(x, y) = 110$$

$$\bar{y} = 30\%$$

$$\sigma_y^2 = 300$$

$$\rho = \frac{\text{Cov}(x, y)}{\sigma_x \sigma_y} = \frac{110}{\sqrt{41} \sqrt{300}} = 2.68 \Rightarrow \text{aggressive stock}$$

$$a = \bar{y} - b\bar{x}$$

$$= 30 - 2.68 \times 27$$

$$= -42.36$$

$$CL = \boxed{R_i^A = -42.36 + 2.68 R_m}$$